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Wolfgang Woess

Denumerable Markov Chains

**Generating Functions
Boundary Theory
Random Walks on Trees**



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