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# **Frobenius Algebras I**

**Basic Representation Theory**



European Mathematical Society

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Mira and Taeko  
and children  
Magda, Akiko, Ikuo and Taketo*