# EMS Tracts in Mathematics 19

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# Infinitesimal Geometry of Quasiconformal and Bi-Lipschitz Mappings in the Plane



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