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Andrzej Skowroński
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Frobenius Algebras II

Tilted and Hochschild Extension Algebras



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Authors:

Andrzej Skowroński
Faculty of Mathematics
and Computer Science
Nicolaus Copernicus University
Chopina 12/18
87-100 Toruń
Poland

E-mail: skowron@mat.uni.torun.pl

Kunio Yamagata
Department of Mathematics
Tokyo University of Agriculture
and Technology
Nakacho 2-24-16, Koganei
Tokyo 184-8588
Japan

E-mail: yamagata@cc.tuat.ac.jp

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Contact address:

European Mathematical Society Publishing House
Seminar for Applied Mathematics
ETH-Zentrum SEW A21
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Mira and Taeko
and children
Magda, Akiko, Ikuo and Taketo*