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Estimates for Differential Operators in Half–space

Translated from the German by
Darya Apushkinskaya

European Mathematical Society

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Dedicated to
Solomon Grigorievich Mikhlin

When a problem about partial differential operators has been fitted into the abstract theory, all that remains is usually to prove a suitable inequality and much of our new knowledge is, in fact, essentially contained in such inequalities. But the abstract theory is not only a tool, it is also a guide to general and fruitful problems.

Lars Gårding