

EMS Tracts in Mathematics 33

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Sergey I. Repin
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Accuracy of Mathematical Models

Dimension Reduction,
Homogenization, and Simplification



European Mathematical Society

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2010 Mathematical Subject Classification (primary; secondary): 35-02; 35J20, 35J50, 35J60, 35J88, 49M29, 65N15, 65N85, 74K20

Key words: Modelling error, *a posteriori* error majorant, model simplification, dimension reduction, homogenization, conversion of models

ISBN 978-3-03719-206-1

The Swiss National Library lists this publication in The Swiss Book, the Swiss national bibliography, and the detailed bibliographic data are available on the Internet at <http://www.helvetica.ch>.

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Contact address:

European Mathematical Society – EMS – Publishing House
Institut für Mathematik
Technische Universität Berlin
Straße des 17. Juni 136
10623 Berlin
Germany

info@ems.press
<https://ems.press>

Typeset using the authors' T_EX files: le-tex publishing services GmbH, Leipzig, Germany
Printing and binding: Beltz Bad Langensalza GmbH, Bad Langensalza, Germany

∞ Printed on acid-free paper

9 8 7 6 5 4 3 2 1

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