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Edited by Ari Laptev (Imperial College, London, UK)

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Ciro Ciliberto

# Classification of Complex Algebraic Surfaces



European Mathematical Society

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