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Alessio Figalli  
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**An Invitation to  
Optimal Transport,  
Wasserstein Distances,  
and Gradient Flows**



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