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Edited by Ari Laptev (Imperial College, London, UK)

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Orthogonal Polynomials and Linear Functionals

An Algebraic Approach and Applications



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