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Piermarco Cannarsa

Filippo Gazzola

Dynamic Optimization for Beginners

With Prerequisites and Applications



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To Francesca and Chiara.