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Olivier Lablée

**Spectral
Theory in
Riemannian
Geometry**



European Mathematical Society

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Olivier Lablée