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Edited by Andrew Ranicki (University of Edinburgh, U.K.)

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Basic Noncommutative Geometry

Second edition



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