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Nils Berglund

# An Introduction to Singular Stochastic PDEs

## Allen–Cahn Equations, Metastability, and Regularity Structures

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To Anne Dudley, Gary Langan, J. J. Jeczalik, and Martin Hairer,
for teaching us the Art of Noise