

# List of themes

For readers who want to acquaint themselves with the various facets of Elliott Lieb's work, we have compiled an (incomplete) list of themes he has worked on and of theorems and models that are named after him. Many, but not all are covered by some chapters in the present two volumes. The titles are followed by two lists of chapter numbers, separated by a semicolon. Numbers before the semicolon refer to chapters where the corresponding topic is a main focus. Numbers after the semicolon refer to secondary appearances.

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