

**ICM 1998**  
**CONTENTS OF VOLUMES I, II, AND III**

Preface .....	I	11
Past Congresses .....	I	12
Past Fields Medalists and Rolf Nevanlinna Prize Winners .....	I	13
MARTIN GRÖTSCHEL: Organization of the Congress .....	I	15
The Committees of the Congress .....	I	19
List of Donors .....	I	21
Opening Ceremony .....	I	23
YURI I. MANIN: Presentation of the Fields Medals and a Special Tribute .....	I	45
DAVID MUMFORD: Presentation of the Rolf Nevanlinna Prize .....	I	49
Fax to the Federal President and to the Governing Mayor .....	I	50
Closing Ceremony .....	I	53
List of Participants .....	I	61
Participants by Country .....	I	96

**THE WORK OF THE FIELDS MEDALISTS  
AND OF THE ROLF NEVANLINNA PRIZE WINNER**

PETER GODDARD: The Work of Richard Ewen Borcherds .....	I	99
BÉLA BOLLOBÁS: The Work of William Timothy Gowers .....	I	109
CLIFFORD HENRY TAUBES: The Work of Maxim Kontsevich .....	I	119
STEVE SMALE: The Work of Curtis T. McMullen .....	I	127
RONALD GRAHAM: The Work of Peter W. Shor .....	I	133

**INVITED ONE-HOUR PLENARY LECTURES**

JEAN-MICHEL BISMUT: Local Index Theory and Higher Analytic Torsion .....	I	143
CHRISTOPHER DENINGER: Some Analogies Between Number Theory and Dynamical Systems on Foliated Spaces .....	I	163
PERSI DIACONIS: From Shuffling Cards to Walking Around the Building: An Introduction to Modern Markov Chain Theory .....	I	187
GIOVANNI GALLAVOTTI: Chaotic Hypothesis and Universal Large Deviations Properties .....	I	205
WOLFGANG HACKBUSCH: From Classical Numerical Mathematics to Scientific Computing .....	I	235
HELMUT H. W. HOFER: Dynamics, Topology, and Holomorphic Curves .....	I	255
EHUD HRUSHOVSKI: Geometric Model Theory .....	I	281
I. G. MACDONALD: Constant Term Identities, Orthogonal Polynomials, and Affine Hecke Algebras .....	I	303
STÉPHANE MALLAT: Applied Mathematics Meets Signal Processing ..	I	319
DUSA McDUFF: Fibrations in Symplectic Topology .....	I	339

TETSUJI MIWA: Solvable Lattice Models and Representation Theory of Quantum Affine Algebras .....	I	359
JÜRGEN MOSER: Dynamical Systems – Past and Present .....	I	381
GEORGE PAPANICOLAOU: Mathematical Problems in Geophysical Wave Propagation .....	I	403
GILLES PISIER: Operator Spaces and Similarity Problems .....	I	429
PETER SARNAK: L-Functions .....	I	453
PETER W. SHOR: Quantum Computing .....	I	467
KARL SIGMUND: The Population Dynamics of Conflict and Cooperation .....	I	487
MICHEL TALAGRAND: Huge Random Structures and Mean Field Models for Spin Glasses .....	I	507
CUMRUN VAFA: Geometric Physics .....	I	537
MARCELO VIANA: Dynamics: A Probabilistic and Geometric Perspective .....	I	557
VLADIMIR VOEVODSKY: $\mathbf{A}^1$ -Homotopy Theory .....	I	579

**LECTURES BY THE FIELDS MEDALISTS  
AND BY THE ROLF NEVANLINNA PRIZE WINNER**

RICHARD E. BORCHERDS: What is Moonshine? .....	I	607
W. T. GOWERS: Fourier Analysis and Szemerédi's Theorem .....	I	617
CURTIS T. McMULLEN: Rigidity and Inflexibility in Conformal Dynamics .....	II	841
see also: .....	I	630
PETER W. SHOR: Quantum Computing .....	I	467

**APPENDIX: INVITED FORTY-FIVE MINUTE LECTURES  
AT THE SECTION MEETINGS**

This appendix contains three manuscripts of Invited Speakers which are not included in Volume II or III

**SECTION 1. LOGIC:**

A. J. WILKIE: O-Minimality .....	I	633
----------------------------------	---	-----

**SECTION 10. PARTIAL DIFFERENTIAL EQUATIONS:**

MIKHAIL SAFONOV: Estimates Near the Boundary for Solutions of Second Order Parabolic Equations .....	I	637
--	---	-----

**SECTION 12. PROBABILITY AND STATISTICS:**

F. GÖTZE: Errata: Lattice Point Problems .....	I	648
--	---	-----

**SECTION 16. APPLICATIONS:**

SERAFIM BATZOGLOU, BONNIE BERGER, DANIEL J. KLEITMAN, ERIC S. LANDER, AND LIOR PACHTER: Recent Developments in Computational Gene Recognition .....	I	649
---	---	-----

<b>AUTHOR INDEX FOR VOLUMES I, II, AND III .....</b>	I	659
--	---	-----

**INVITED FORTY-FIVE MINUTE LECTURES  
AT THE SECTION MEETINGS  
CONTENTS OF VOLUMES II AND III**

In case of several authors, Invited Speakers are marked with a \*.  
The author index is at the end of each of these two volumes.

**SECTION 1. LOGIC**

MATTHEW FOREMAN: Generic Large Cardinals: New Axioms for Mathematics?	II	11
GREG HJORTH: When is an Equivalence Relation Classifiable?	II	23
LUDOMIR NEWELSKI: Meager Forking and m-Independence	II	33
STEVO TODORCEVIC: Basis Problems in Combinatorial Set Theory ..	II	43

**SECTION 2. ALGEBRA**

ERIC M. FRIEDLANDER: Geometry of Infinitesimal Group Schemes ..	II	55
SERGEI V. IVANOV: On the Burnside Problem for Groups of Even Exponent .....	II	67
WILLIAM M. KANTOR: Simple Groups in Computational Group Theory .....	II	77
GUNTER MALLE: Spetses .....	II	87
ALEKSANDR V. PUKHLIKOV: Birational Automorphisms of Higher-Dimensional Algebraic Varieties .....	II	97
IDUN REITEN: Tilting Theory and Quasitilted Algebras .....	II	109
JEREMY RICKARD: The Abelian Defect Group Conjecture .....	II	121
ANER SHALEV: Simple Groups, Permutation Groups, and Probability ..	II	129

**SECTION 3. NUMBER THEORY AND ARITHMETIC ALGEBRAIC GEOMETRY**

VLADIMIR G. BERKOVICH: p-Adic Analytic Spaces .....	II	141
PIERRE COLMEZ: Représentations p-adiques d'un Corps Local .....	II	153
W. DUKE: Bounds for Arithmetic Multiplicities .....	II	163
FRANÇOIS GRAMAIN: Quelques Résultats d'Indépendance Algébrique .....	II	173
LOÏC MEREL: Points Rationnels et Séries de Dirichlet .....	II	183
SHINICHI MOCHIZUKI: The Intrinsic Hodge Theory of p-Adic Hyperbolic Curves .....	II	187
HANS PETER SCHLICKEWEI: The Subspace Theorem and Applications .....	II	197
TAKESHI TSUJI: p-Adic Hodge Theory in the Semi-Stable Reduction Case .....	II	207
SHOU-WU ZHANG: Small Points and Arakelov Theory .....	II	217

**SECTION 4. ALGEBRAIC GEOMETRY**

PAUL S. ASPINWALL: String Theory and Duality .....	II	229
VICTOR V. BATYREV: Mirror Symmetry and Toric Geometry .....	II	239
MAURIZIO CORNALBA: Cohomology of Moduli Spaces of Stable Curves ..	II	249

A. J. DE JONG: Barsotti-Tate Groups and Crystals .....	II	259
MARK L. GREEN: Higher Abel-Jacobi Maps .....	II	267
M. KAPRANOV: Operads and Algebraic Geometry .....	II	277

## SECTION 5. DIFFERENTIAL GEOMETRY AND GLOBAL ANALYSIS

DMITRI BURAGO: Hard Balls Gas and Alexandrov Spaces of Curvature Bounded Above .....	II	289
TOBIAS H. COLDING: Spaces with Ricci Curvature Bounds .....	II	299
S. K. DONALDSON: Lefschetz Fibrations in Symplectic Geometry ....	II	309
BORIS DUBROVIN: Geometry and Analytic Theory of Frobenius Manifolds .....	II	315
YAKOV ELIASHBERG: Invariants in Contact Topology .....	II	327
S. GALLOT: Curvature-Decreasing Maps are Volume-Decreasing .....	II	339
GERHARD HUISKEN: Evolution of Hypersurfaces by Their Curvature in Riemannian Manifolds .....	II	349
DOMINIC JOYCE: Compact Manifolds with Exceptional Holonomy ....	II	361
FRANÇOIS LABOURIE: Large Groups Actions on Manifolds .....	II	371
JOACHIM LOHKAMP: Curvature Contents of Geometric Spaces .....	II	381
FRANZ PEDIT AND ULRICH PINKALL*: Quaternionic Analysis on Riemann Surfaces and Differential Geometry .....	II	389
LEONID POLTEROVICH: Geometry on the Group of Hamiltonian Diffeomorphisms .....	II	401
YONGBIN RUAN: Quantum Cohomology and its Application .....	II	411

## SECTION 6. TOPOLOGY

A. N. DRANISHNIKOV: Dimension Theory and Large Riemannian Manifolds .....	II	423
W. G. DWYER: Lie Groups and p-Compact Groups .....	II	433
RONALD FINTUSHEL* AND RONALD J. STERN*: Constructions of Smooth 4-Manifolds .....	II	443
MICHAEL H. FREEDMAN: Topological Views on Computational Complexity .....	II	453
MARK MAHOWALD: Toward a Global Understanding of $\pi_*(S^n)$ ....	II	465
TOMOTADA OHTSUKI: A Filtration of the Set of Integral Homology 3-Spheres .....	II	473
BOB OLIVER: Vector Bundles over Classifying Spaces .....	II	483
CLIFFORD HENRY TAUBES: The Geometry of the Seiberg-Witten Invariants .....	II	493

## SECTION 7. LIE GROUPS AND LIE ALGEBRAS

JAMES ARTHUR: Towards a Stable Trace Formula .....	II	507
JOSEPH BERNSTEIN: Analytic Structures on Representation Spaces of Reductive Groups .....	II	519
IVAN CHEREDNIK: From Double Hecke Algebra to Analysis .....	II	527
ALEX ESKIN: Counting Problems and Semisimple Groups .....	II	539

## CONTENTS

5

ROBERT E. KOTTWITZ: Harmonic Analysis on Semisimple p-Adic Lie Algebras .....	II	553
L. LAFFORGUE: Chtoucas de Drinfeld et Applications .....	II	563
SHAHAR MOZES: Products of Trees, Lattices and Simple Groups .....	II	571
VERA SERGANOVÁ: Characters of Irreducible Representations of Simple Lie Superalgebras .....	II	583
KARI VILONEN: Topological Methods in Representation Theory .....	II	595
MINORU WAKIMOTO: Representation Theory of Affine Superalgebras at the Critical Level .....	II	605

## SECTION 8. ANALYSIS

KARI ASTALA: Analytic Aspects of Quasiconformality .....	II	617
MICHAEL CHRIST: Singularity and Regularity — Local and Global ...	II	627
NIGEL HIGSON: The Baum-Connes Conjecture .....	II	637
MICHAEL T. LACEY: On the Bilinear Hilbert Transform .....	II	647
PERTTI MATTILA: Rectifiability, Analytic Capacity, and Singular Integrals .....	II	657
VITALI MILMAN: Randomness and Pattern in Convex Geometric Analysis .....	II	665
DETLEF MÜLLER: Functional Calculus on Lie Groups and Wave Propagation .....	II	679
STEFAN MÜLLER* AND VLADIMÍR ŠVERÁK: Unexpected Solutions of First and Second Order Partial Differential Equations .....	II	691
KLAS DIEDERICH AND SERGEY PINCHUK*: Reflection Principle in Higher Dimensions .....	II	703
KRISTIAN SEIP: Developments from Nonharmonic Fourier Series .....	II	713
HART F. SMITH: Wave Equations with Low Regularity Coefficients ..	II	723
NICOLE TOMCZAK-JAEGERMANN: From Finite- to Infinite-Dimensional Phenomena in Geometric Functional Analysis on Local and Asymptotic Levels .....	II	731
STEPHEN WAINGER: Discrete Analogues of Singular and Maximal Radon Transforms .....	II	743
THOMAS WOLFF: Maximal Averages and Packing of One Dimensional Sets .....	II	755

## SECTION 9. ORDINARY DIFFERENTIAL EQUATIONS AND DYNAMICAL SYSTEMS

W. DE MELO: Rigidity and Renormalization in One Dimensional Dynamical Systems .....	II	765
L. H. ELIASSON: Reducibility and Point Spectrum for Linear Quasi-Periodic Skew-Products .....	II	779
SHUHEI HAYASHI: Hyperbolicity, Stability, and the Creation of Homoclinic Points .....	II	789
MICHAEL HERMAN: Some Open Problems in Dynamical Systems ...	II	797
YURI KIFER: Random Dynamics and its Applications .....	II	809

SERGEI B. KUJSIN: Elements of a Qualitative Theory of Hamiltonian PDEs .....	II	819
KRYSTYNA KUPERBERG: Counterexamples to the Seifert Conjecture .	II	831
CURTIS T. McMULLEN: Rigidity and Inflexibility in Conformal Dynamics .....	II	841
GRZEGORZ ŚWIĘTEK: Induced Hyperbolicity for One-Dimensional Maps .....	II	857
ZHIHONG XIA: Arnold Diffusion: A Variational Construction .....	II	867
<b>SECTION 10. PARTIAL DIFFERENTIAL EQUATIONS</b>		
FABRICE BETHUEL: Vortices in Ginzburg-Landau Equations .....	III	11
FRÉDÉRIC HÉLEIN: Phenomena of Compensation and Estimates for Partial Differential Equations .....	III	21
ROBERT R. JENSEN: Viscosity Solutions of Elliptic Partial Differential Equations .....	III	31
HANS LINDBLAD: Minimal Regularity Solutions of Nonlinear Wave Equations .....	III	39
M. MACHEDON: Fourier Analysis of Null Forms and Non-linear Wave Equations .....	III	49
FRANK MERLE: Blow-up Phenomena for Critical Nonlinear Schrödinger and Zakharov Equations .....	III	57
GUSTAVO PONCE: On Nonlinear Dispersive Equations .....	III	67
GUNTHER UHLMANN: Inverse Boundary Value Problems for Partial Differential Equations .....	III	77
D. YAFAEV: Scattering Theory: Some Old and New Problems .....	III	87
<b>SECTION 11. MATHEMATICAL PHYSICS</b>		
EUGENE BOGOMOLNY: Spectral Statistics .....	III	99
DETLEV BUCHHOLZ: Scaling Algebras in Local Relativistic Quantum Physics .....	III	109
J. T. CHAYES: Finite-Size Scaling in Percolation .....	III	113
P. COLLET: Extended Dynamical Systems .....	III	123
ROBBERT DIJKGRAAF: The Mathematics of Fivebranes .....	III	133
ANTONIO GIORGILLI: On the Problem of Stability for Near to Integrable Hamiltonian Systems .....	III	143
GIAN MICHELE GRAF: Stability of Matter in Classical and Quantized Fields .....	III	153
ALEXANDER BERKOVICH AND BARRY M. MCCOY*: Rogers-Ramanujan Identities: A Century of Progress from Mathematics to Physics .....	III	163
ROBERTO H. SCHONMANN: Metastability and the Ising Model .....	III	173
FEODOR A. SMIRNOV: Space of Local Fields in Integrable Field Theory and Deformed Abelian Differentials .....	III	183
HORNG-TZER YAU: Scaling Limit of Particle Systems, Incompressible Navier-Stokes Equation and Boltzmann Equation .....	III	193

## SECTION 12. PROBABILITY AND STATISTICS

DAVID J. ALDOUS: Stochastic Coalescence .....	III	205
MAURY BRAMSON: State Space Collapse for Queueing Networks .....	III	213
MARK I. FREIDLIN: Random and Deterministic Perturbations of Nonlinear Oscillators .....	III	223
JAYANTA K. GHOSH: Bayesian Density Estimation .....	III	237
F. GÖTZE: Lattice Point Problems and the Central Limit Theorem in Euclidean Spaces .....	III	245
PETER HALL* AND BRETT PRESNELL: Applications of Intentionally Biased Bootstrap Methods .....	III	257
IAIN M. JOHNSTONE: Oracle Inequalities and Nonparametric Function Estimation .....	III	267
JEAN-FRANÇOIS LE GALL: Branching Processes, Random Trees and Superprocesses .....	III	279
DAVID SIEGMUND: Genetic Linkage Analysis: an Irregular Statistical Problem .....	III	291
ALAIN-SOL SZNITMAN: Brownian Motion and Random Obstacles ....	III	301
BORIS TSIRELSON: Within and Beyond the Reach of Brownian Innovation .....	III	311
R. J. WILLIAMS: Reflecting Diffusions and Queueing Networks .....	III	321

## SECTION 13. COMBINATORICS

BÉLA BOLLOBÁS: Hereditary Properties of Graphs: Asymptotic Enumeration, Global Structure, and Colouring .....	III	333
ANDRÁS FRANK: Applications of Relaxed Submodularity .....	III	343
ALAIN LASCOUX: Ordonner le Groupe Symétrique: Pourquoi Utiliser l'Algèbre de Iwahori-Hecke ? .....	III	355
JIŘÍ MATOUŠEK: Mathematical Snapshots from the Computational Geometry Landscape .....	III	365
HARALD NIEDERREITER: Nets, $(t, s)$ -Sequences, and Algebraic Curves over Finite Fields with Many Rational Points .....	III	377
N. J. A. SLOANE: The Sphere Packing Problem .....	III	387
JOSEPH A. THAS: Finite Geometries, Varieties and Codes .....	III	397
ANDREI ZELEVINSKY: Multisegment Duality, Canonical Bases and Total Positivity .....	III	409

## SECTION 14. MATHEMATICAL ASPECTS OF COMPUTER SCIENCE

MIKLÓS AJTAI: Worst-Case Complexity, Average-Case Complexity and Lattice Problems .....	III	421
JOAN FEIGENBAUM: Games, Complexity Classes, and Approximation Algorithms .....	III	429
JOHAN HÅSTAD: On Approximating NP-Hard Optimization Problems	III	441
TONIANN PITASSI: Unsolvable Systems of Equations and Proof Complexity .....	III	451
MADHU SUDAN: Probabilistic Verification of Proofs .....	III	461

ARTUR ANDRZEJAK AND EMO WELZL\*: Halving Point Sets ..... III 471

#### SECTION 15. NUMERICAL ANALYSIS AND SCIENTIFIC COMPUTING

GREGORY BEYLKIN: On Multiresolution Methods in Numerical Analysis .....	III	481
P. DEIFT*, T. KRIECHERBAUER, K. T-R McLAUGHLIN, S. VENAKIDES AND X. ZHOU: Uniform Asymptotics for Orthogonal Polynomials .....	III	491
BJORN ENGQUIST: Wavelet Based Numerical Homogenization .....	III	503
HISASHI OKAMOTO: A Study of Bifurcation of Kolmogorov Flows with an Emphasis on the Singular Limit .....	III	513
JAN-OLOV STRÖMBERG: Computation with Wavelets in Higher Dimensions .....	III	523
LLOYD N. TREFETHEN* AND TOBIN A. DRISCOLL: Schwarz–Christoffel Mapping in the Computer Era .....	III	533

#### SECTION 16. APPLICATIONS

MARCO AVELLANEDA: The Minimum-Entropy Algorithm and Related Methods for Calibrating Asset-Pricing Models .....	III	545
ANDREAS DRESS*, WERNER TERHALLE: The Tree of Life and Other Affine Buildings .....	III	565
LESLIE GREENGARD* AND XIAOBAI SUN: A New Version of the Fast Gauss Transform .....	III	575
ULF GRENANDER: Strategies for Seeing .....	III	585
FRANK HOPPENSTEADT* AND EUGENE IZHKEVICH: Canonical Models in Mathematical Neuroscience .....	III	593
THOMAS YIZHAO HOU: Numerical Study of Free Interface Problems Using Boundary Integral Methods .....	III	601
GÉRARD IOSS: Travelling Water-Waves, as a Paradigm for Bifurcations in Reversible Infinite Dimensional “Dynamical” Systems	III	611
YURY GRABOVSKY AND GRAEME W. MILTON*: Exact Relations for Composites: Towards a Complete Solution .....	III	623
CHARLES S. PESKIN: Optimal Dynamic Instability of Microtubules ..	III	633

#### SECTION 17. CONTROL THEORY AND OPTIMIZATION

DAVID APPLEGATE, ROBERT BIXBY, VAŠEK CHV'ATAL AND WILLIAM COOK*: On the Solution of Traveling Salesman Problems	III	645
MICHEL X. GOEMANS: Semidefinite Programming and Combinatorial Optimization .....	III	657
RICHARD H. BYRD AND JORGE NOCEDAL*: Active Set and Interior Methods for Nonlinear Optimization .....	III	667
RANGA ANBIL, JOHN J. FORREST AND WILLIAM R. PULLEYBLANK*: Column Generation and the Airline Crew Pairing Problem .....	III	677

ALEXANDER SCHRIJVER: Routing and Timetabling by Topological Search .....	III	687
JAN C. WILLEMS: Open Dynamical Systems and their Control .....	III	697
MICHAL KOČVARA AND JOCHEM ZOWE*: Free Material Optimization	III	707
<b>SECTION 18. TEACHING AND POPULARIZATION OF MATHEMATICS</b>		
GEORGE E. ANDREWS: Mathematics Education: Reform or Renewal? III		719
MICHELE ARTIGUE: De la Comprehension des Processus d'Apprentissage à la Conception de Processus d'Enseignement .....	III	723
MARIA G. BARTOLINI BUSSI: Drawing Instruments: Theories and Practices from History to Didactics .....	III	735
MIGUEL DE GUZMÁN*, BERNARD R. HODGSON*, ALINE ROBERT* AND VINICIO VILLANI*: Difficulties in the Passage from Secondary to Tertiary Education .....	III	747
D. J. LEWIS: Mathematics Instruction in the Twenty-first Century ..	III	763
MOGENS NISS: Aspects of the Nature and State of Research in Mathematics Education .....	III	767
DAVID A. SMITH: Renewal in Collegiate Mathematics Education .....	III	777
<b>SECTION 19. HISTORY OF MATHEMATICS</b>		
KARINE CHEMLA: History of Mathematics in China: A Factor in World History and a Source for New Questions .....	III	789
JOSEPH W. DAUBEN: Marx, Mao and Mathematics: The Politics of Infinitesimals .....	III	799
JEREMY J GRAY: The Riemann-Roch Theorem and Geometry, 1854-1914 .....	III	811

