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Alessio Figalli
Federico Glaudo

**An Invitation to
Optimal Transport,
Wasserstein Distances,
and Gradient Flows**
Second Edition



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Authors

Alessio Figalli
Department of Mathematics
ETH Zürich
Rämistrasse 101
8092 Zürich, Switzerland
Email: alessio.figalli@math.ethz.ch

Federico Glaudo
School of Mathematics
Institute for Advanced Study
Einstein Drive 1
Princeton, NJ 08540, USA
Email: fglaudo@ias.edu

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