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Partial Differential Equations, Spectral Theory, and Mathematical Physics

The Ari Laptev Anniversary Volume

Edited by

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Rupert L. Frank

Fritz Gesztesy

Helge Holden

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Editors:

Pavel Exner

Doppler Institute for Mathematical Physics and Applied Mathematics, Czech Technical University, Břehová 7, 11519 Prague, Czech Republic; and Department of Theoretical Physics, Nuclear Physics Institute, Czech Academy of Sciences, 25068 Řež, Czech Republic
E-mail: exner@ujf.cas.cz

Rupert L. Frank

Department of Mathematics, California Institute of Technology, Pasadena, CA 91125, USA; and Mathematisches Institut, Ludwig-Maximilians-Universität München, Theresienstraße 39, 80333 München, Germany
E-mail: rlfrank@caltech.edu

Fritz Gesztesy

Department of Mathematics, Baylor University, Sid Richardson Bldg., 1410 S. 4th Street, Waco, TX 76706, USA
E-mail: fritz_gesztesy@baylor.edu

Helge Holden

Department of Mathematical Sciences, Norwegian University of Science and Technology, Alfred Getz vei 1, 7491 Trondheim, Norway
E-mail: helge.holden@ntnu.no

Timo Weidl

Institut für Analysis, Dynamik und Modellierung, Fakultät für Mathematik und Physik, Universität Stuttgart, Pfaffenwaldring 57, 70569 Stuttgart, Germany
E-mail: weidl@mathematik.uni-stuttgart.de

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