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## Tomas Dominguez Jean-Christophe Mourrat

# Statistical Mechanics of Mean-Field Disordered Systems

A Hamilton-Jacobi Approach



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