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Edited by Ari Laptev (Imperial College, London, UK)

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Umberto Zannier

# Lecture Notes on Diophantine Analysis

With an Appendix by Francesco Amoroso

Second Edition



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