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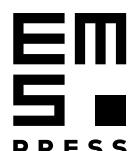
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Fabrice Baudoin

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# Stochastic Areas, Horizontal Brownian Motions, and Hypoelliptic Heat Kernels



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