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# **Tractability of Multivariate Problems**

## **Volume III: Standard Information for Operators**



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