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## **EMS Tracts in Mathematics**

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## Tractability of Multivariate Problems

## Volume I: Linear Information



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For (für) Gabi. Most likely, she will not solve any of the open problems but you never know.

For (dla) my grandson Filip Woźniakowski and his parents Agnieszka and Artur.

> Today, Filip is only two years old. But we hope that one day he will read the book and solve some of the remaining open problems.