

EMS Tracts in Mathematics 12

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Tractability of Multivariate Problems

Volume II: Standard Information for Functionals



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For (für) my parents Esther and Heinz.

For (dla) my grandson Mateusz Woźniakowski.

Today, Mateusz is almost two years old.

But we hope that one day he will read

the book and join his older brother

Filip in solving some of the

remaining open problems.