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Camillo De Lellis

Matteo Focardi

The Regularity Theory for the Mumford–Shah Functional on the Plane



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