

Erratum to “The line bundles on moduli stacks of principal bundles on a curve”

Indranil Biswas and Norbert Hoffmann

Abstract. A missing hypothesis is added to Lemma 2.2.1 in [Doc. Math. 15 (2010), 35–72]. The rest of the text remains unchanged.

We thank Sergey Lysenko, Stefan Reppen, and Archia Ghasabadi for pointing out that Lemma 2.2.1 in [1] is incorrect as stated. For example, if $G_1 = G_2 = 1$ is the trivial group, then also $H = 1$, and hence $\mathcal{M}_H \cong \text{Spec}(k)$ is just a point, whereas $\mathcal{M}_{G_1} \times_{\mathcal{M}_G} \mathcal{M}_{G_2} \cong G$. The problem with the argument in [1] is that the scheme F constructed there might not be faithfully flat over X .

To rectify this, we add the hypothesis to Lemma 2.2.1 in [1] that one of the two groups G_1 and G_2 , say G_2 , is faithfully flat over G . Then E_2 is faithfully flat over E , and therefore F is faithfully flat over E_1 and thus also over X , so F is indeed a principal H -bundle over X , and the lemma follows.

Since this extra hypothesis is satisfied wherever Lemma 2.2.1 is used in [1], the rest of the paper is not affected.

References

- [1] I. Biswas and N. Hoffmann, [The line bundles on moduli stacks of principal bundles on a curve](#). *Doc. Math.* **15** (2010), 35–72 Zbl 1193.14009 MR 2628848

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Indranil Biswas

Department of Mathematics, Shiv Nadar University, NH91, Tehsil Dadri, Greater Noida, Uttar Pradesh 201314, India; indranil.biswas@snu.edu.in, indranil29@gmail.com

Norbert Hoffmann

Department of Mathematics and Computer Studies, Mary Immaculate College, South Circular Road, Limerick V94 VN26, Ireland; norbert.hoffmann@mic.ul.ie

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