

Supplement to ‘Weakly 1-Complete Manifold and Levi Problem’

By

Takeo OHSAWA*

In the proof of Theorem 2.1 in [3] there is a gap which seems difficult to be filled by an elementary argument. Here we shall fill it with the aid of Cartan’s theorem and Norguet-Siu’s theorem.

Let the notations be as in Theorem 2.1 [3]. In the proof, we have shown that, by induction, for any $x \in \partial X_c$, for any hyperplane H in \mathbb{P}^n , and for any sequence $\{x_k\}$ in $\pi^{-1}(H) \cap X_c$ such that $x_k \rightarrow x$, there is a holomorphic function f on X_c such that

$$\lim_{x_k \rightarrow x} |f(x_k)| = \infty.$$

But it is too rude to conclude only from this fact that X_c is holomorphically convex. We fill this gap as follows: By the same argument, using the Nakano’s vanishing theorem and the induction, we can prove that for any two points $x, y \in X_c$, either x and y are contained in a connected compact analytic subset of X_c , or there is a holomorphic function on X_c which separates them. Let R be the equivalence relation defined on X_c by the following rule: $x \sim x'$ if and only if $f(x) = f(x')$ for any holomorphic function f on X_c . Then the fibers, the equivalence classes of R , are compact and φ is constant on any fiber. Therefore R is a proper relation in Cartan’s sense. Hence, by Main Theorem in [1], there is an analytic space \hat{X}_c and a proper surjective holomorphic map p from X_c to \hat{X}_c . Clearly, $1/(c - \varphi \circ p^{-1})$ is a well defined continuous exhaustion function on \hat{X}_c which is plurisubharmonic on the regular points of \hat{X}_c .

Therefore, applying the theorem of Norguet-Siu (cf. Theorem 2 in [2]), we obtain the Steinness of \hat{X}_c , whence follows the holomorphical convexity of X_c . The same argument can be applied to prove the holomorphical convexity of

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* Research Institute for Mathematical Sciences, Kyoto University, Kyoto 606, Japan.

the weakly 1-complete domains over hyperquadrics, complete intersections of type (2, 2), and hypercubics.

References

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